

Physics

Q.1 A ball is thrown from ground with velocity u and angle θ with horizontal. Its horizontal range is 10m. If the ball is thrown with velocity $3u$ and with same angle θ , the horizontal range will become

Option 1:

10 m

Option 2:

40 m

Option 3:

90 m

Option 4:

60 m

Correct Answer:

90 m

Solution:

As we learned

Projectile Projected at angle θ -

When the velocity of projectile increased n time then

- wherein

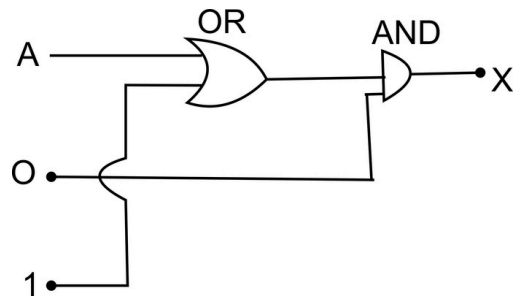
horizontal range is increased by a factor of n^2

$$R = \frac{u^2 \sin 2\theta}{g}$$

for same θ

$$R \propto u^2 \quad \frac{R_2}{R_1} = \left(\frac{3u}{u}\right)^2 \Rightarrow R_2 = 9R_1$$

Q. 2 The output, in the following gate logic, would be:



Option 1:

0

Option 2:

1

Option 3:

A

Option 4:

$1 + A$

Correct Answer:

0

Solution:

As we have learned

Some Important relation -

$$A + A = A$$

$$A \cdot A = A$$

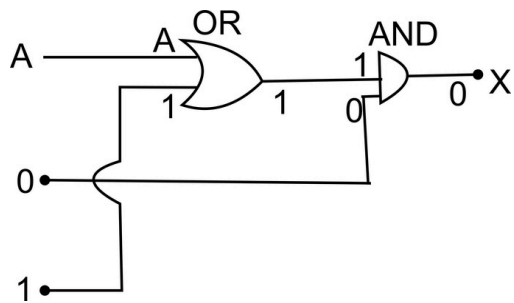
$$A + 1 = 1$$

$$A \cdot 1 = A$$

$$A \cdot 0 = 0$$

$$A + 0 = A$$

-



We know $1+A=1$ always, hence the output of OR gate would be a

	A	OR
1	0	
1	1	1
1	1	1

Similar $1+0 \neq 0$

We know that output of AND gate is zero, if atleast one input to

A		AND
1	0	0
0	0	0

Hence $X=0$

Q. 3 If the magnitude of voltage in a circuit changes with time and direction changes periodically then the voltage is called:

Option 1:

Alternative voltage

Option 2:

direct voltage

Option 3:

constant voltage

Option 4:

reversible voltage

Correct Answer:

Alternative voltage

Solution:

As we learn

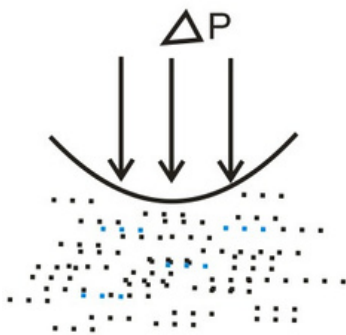
Alternating Voltage (V) -

An alternating voltage (V) is one whose magnitude changes with time between zero to peak value (0 to V_0)

- w h e r e i n

Where voltage changes periodically.

Q. 4 For the gluon concave surface ΔP the excess oressure



Option 1:

Zero

Option 2:

$$\frac{T}{R}$$

Option 3:

$$\frac{2T}{R}$$

Option 4:

$$\frac{4T}{R}$$

Correct Answer:

$$\frac{2T}{R}$$

Solution:

As we have learnt in

Excess pressure for concave surface -

$$\Delta P = \frac{2T}{R}$$

-

$$\Delta P \text{ for concave } \frac{2T}{R} \text{ surface} =$$

Q. 5 Faraday's law of electromagnetic induction is conservation of

Option 1:

charge

Option 2:

magnetic flux

Option 3:

energy

Option 4:

magnetic field

Correct Answer:

energy

Solution:

As we have learnt

Faraday Second Law of Induction emf -

$$\varepsilon = \frac{-d\phi}{dt} = -L \frac{dI}{dt}$$

-

(concept not mentioned)

Induced charge is given by the rate of change of magnetic flux

Q. 6 Which of the following is true about the mass of the body

Option 1:

It's value does not change with g

Option 2:

It is a scalar quantity

Option 3:

it's unit is in kilogram

Option 4:

All of the above

Correct Answer:

All of the above

Solution:

As we learn

Mass -

Quantity of matter contained in body

S.I. $\rightarrow [Kg]$

dimension $[M]$

- wherein

(i) Value does not change with g

(ii) Can never be zero

(iii) Scalar quantity

Q. 7 A constant retarding force of 50m is applied to a body of speed of 15m/s. How long does the body take to stop ?

Option 1:

4 s

Option 2:

5 s

Option 3:

10 s

Option 4:

6 s

Correct Answer:

6 s

Solution:

As we learn

Newton's 2nd Law -

$$F \propto \frac{dp}{dt}$$

$$F = \frac{Kdp}{dt}$$

$$F = \frac{d(mv)}{dt}$$

$$F = \frac{m(dv)}{dt}$$

$$\frac{dv}{dt} = a$$

Therefore $F = ma$

- wherein

$K = 1$ in C.G.S & S.I

Force can be defined as rate of change of momentum.

Retardation $\Rightarrow \frac{F}{m} = \frac{50}{20} = 2.5m/s^2$

Now by equation of motion

$$v = u + at = 0 = u - at$$

$$t = \frac{u}{a} = \frac{15}{2.5} = 6sec$$

Q. 8 If a 5 Kg mass is suspended by a spring balance in a lift with acceleration $a = 2 \text{ m/s}^2$. The reading of the balance is

Option 1:

more than 5Kg weight

Option 2:

is less than 5Kg weight and greater than zero

Option 3:

is equal to 5 Kg weight

Option 4:

zero

Correct Answer:

zero

Solution:

Apparent weight of body in a lift when Lift is moving down with acceleration a

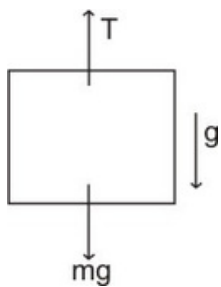
$$a = g$$

$$mg - R = ma$$

$$R = 0$$

Apparent weight = 0 (weightlessness)

Draw FBD of block



$$mg - T = ma$$

$$T = 0$$

so reading of balance is zero

Q. 9 In the experiment of obtaining velocity of transverse wave λ_1 and λ_2 as two successive resonance length then velocity will

Option 1:

$$V \propto (l_1 \times l_2)$$

Option 2:

$$V \propto (l_2/l_1)$$

Option 3:

$$V \propto (l_1/l_2)$$

Option 4:

$$V \propto (l_2 - l_1)$$

Correct Answer:

$$V \propto (l_2 - l_1)$$

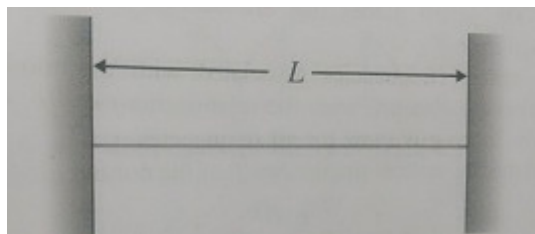
Solution:

As we learned from

Velocity of transverse wave using sonometer -

$$v = n_0 \lambda$$

$$= 2 n_0 (l_2 - l_1)$$



- wherein

$$\text{where } \frac{\lambda}{2} = l_2 - l_1$$

l_2 and l_1 are the two successive resonance length.

$$V = n_0(\lambda)$$

$$\lambda = 2(l_2 - l_1)$$

$$\text{so } V = 2n_0(l_2 - l_1)$$

Q. 10 Axis of rotation of earth is called:

Option 1:

Magnetic axis

Option 2:

Geographic pole

Option 3:

geographic axis

Option 4:

Magnetic pole

Correct Answer:

Geographic pole

Solution:

As we learn

Geographic Axis -

Axis of rotation of Earth is called Geographic axis.

-

Q. 11 The current gain of a common emitter amplifier is 69. If the collector current (in mA) is :

Correct Answer:

6.9

Solution:

As we have learnt,

Relation between α and β -

$$\beta = \frac{\alpha}{1 - \alpha}$$

- wherein

$$\alpha = \frac{I_C}{I_E}$$

$$\beta = \frac{I_C}{I_B} \text{ (current gain)}$$

$$\text{Current gain } \beta = \frac{\Delta I_C}{\Delta I_B} = 69$$

$$\begin{aligned} \frac{\Delta I_C}{\Delta I_E - \Delta I_C} = 69 &\Rightarrow \frac{\Delta I_C}{\Delta I_C} - 1 = \frac{1}{69} \\ \frac{\Delta I_C}{\Delta I_E} = 1 + \frac{1}{69} &= \frac{70}{69} \\ \Rightarrow \Delta I_C = (\Delta I_E) \frac{70}{69} &= (7mA) \times \frac{69}{70} = 6.9mA \end{aligned}$$

Q . 12 A certain mass of hydrogen is changed to He by the process of fusion. The mass defect in fusion reaction is 0.02866u. The energy liberated (in MeV) per μ is ($1\mu=931\text{MeV}$)

Correct Answer:

6 . 6 7 5

Solution:

As we learn

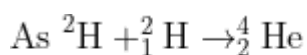
Mass of electron, proton & neutron in terms of energy -

$$m_e = 0.511 \text{ Mev}/c^2$$

$$m_p = 938.27 \text{ Mev}/c^2$$

$$m_n = 939.56 \text{ Mev}/c^2$$

$$1 \text{ amu} = 931.5 \text{ Mev}/c^2$$



Here, $\Delta m = 0.02866\text{u}$

∴ The energy liberated per u is

$$= \frac{\Delta M \times 931}{4} \text{MeV}$$

$$= \frac{0.02866 \times 931}{4} \text{MeV}$$

$$= \frac{26.7}{4} \text{MeV} = 6.675 \text{MeV}$$

Q. 13 When radiation of wavelength λ illuminate a metallic surface, potential is V . When the same surface is illuminated with 3λ , the stopping potential is $V/4$. If the threshold wavelength value of n will be _____

Correct Answer:

9

Solution:

$$\frac{hc}{\lambda} = \frac{hc}{\lambda_0} + eV \quad \dots (i)$$

$$\frac{hc}{3\lambda} = \frac{hc}{\lambda_0} + \frac{e \cdot V}{4} \quad \dots (ii)$$

(multiply equation(ii) by 4)

$$\text{we get } \frac{4hc}{3\lambda} = \frac{4hc}{\lambda_0} + eV \quad \dots (iii)$$

Now From (i) & (iii) we get

$$\frac{hc}{\lambda} - \frac{hc}{\lambda_0} = \frac{4hc}{3\lambda} - \frac{4hc}{\lambda_0}$$

$$-\frac{hc}{3\lambda} = -\frac{3hc}{\lambda_0}$$

$$\Rightarrow 9\lambda = \lambda_0$$

$$n = 9$$

Q. 14 A car is moving with a speed of 30 m/s on a circular path increasing at 2 m/s^2 . What is the acceleration (in m/s^2) of the car?

Correct Answer:

2.7

Solution:

Given :

Tangential acceleration, $(a_t) = 2 \text{ m/s}^2$

Centripetal acceleration, $(a_c) = \frac{v^2}{r} = \frac{900}{500} = 1.8 \text{ m/s}^2$

∴ Net acceleration , $(a) = \sqrt{(a_t)^2 + (a_c)^2}$

$$a = \sqrt{(2)^2 + (1.8)^2} = 2.7 \text{ m/s}^2$$

Q. 15

A man weighs 80 kg. He stands on a weighing scale in a lift which is moving with a uniform acceleration of 5 m/s^2 . What would be the reading on the scale?

Correct Answer:

1200

Solution:

Solution :

Reading of weighing scale = $m(g+a) = 80(10 + 5) = 1200 \text{ N}$

Chemistry

Q. 1 Which of the following is a colourless neutral gas:

Option 1:

NO

Option 2:

NO₂

Option 3:

N₂O₃

Option 4:

N₂O₅

Correct Answer:

NO

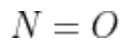
Solution:

As we learn

Nitric oxide -

NO (+2), colourless

- wherein



N_2O : Colourless neutral gas

NO : Colourless neutral gas

NO_2 : Brown gas

N_2O_3 : Blue Solid

N_2O_5 : Colourless solid

Q . 2 A gas expands from 10 ltr to 12 ltr against 1 atm pressure and absorb 10 Ltr – atm heat.
Then change in its internal energy will be

Option 1:

12 Ltr - atm

Option 2:

-2 Ltr – atm

Option 3:

8 Ltr - atm

Option 4:

2 Ltr – atm

Correct Answer:

8 Ltr - atm

Solution:

As we learn

First law of Thermodynamics -

The energy of universe is always conserved or total energy of a

$$\Delta E = q + W$$

- wherein

ΔE = Internal Energy

Q = Heat

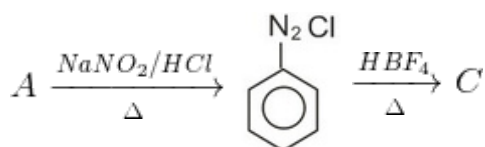
W = work

$$\begin{aligned}\Delta E &= q + w \\ q &= 10 \text{ Ltr-atm} \\ w &= -P(V_f - V_i) \\ &= -1(12 - 10) \\ &= -20 \text{ Ltr-atm}\end{aligned}$$

$$\Delta E = 10 - 20$$

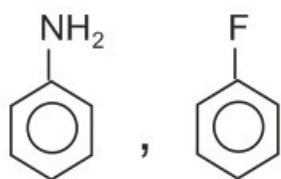
$$\Delta E = -10 \text{ Ltr-atm}$$

Q. 3

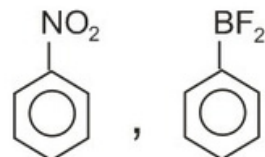


In the above reaction what is A and C respectively?

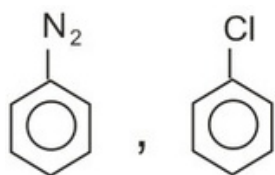
Option 1:



Option 2:



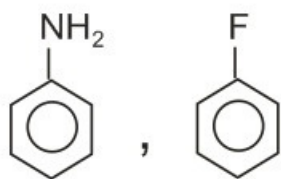
Option 3:



Option 4:

None of these

Correct Answer:



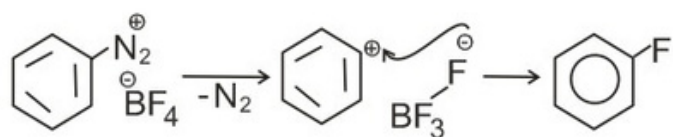
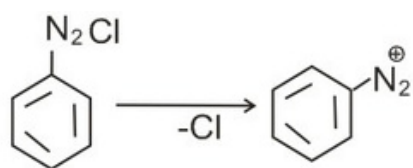
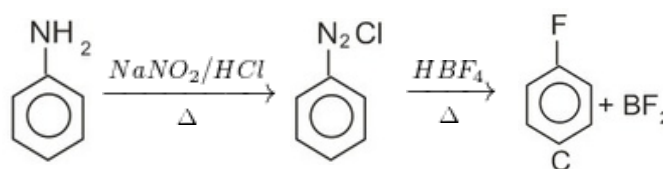
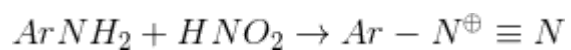
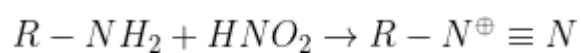
Solution:

As we learn

Reaction with Nitrous Acid Primary Amines -

Primary amines react with nitrous acid to produce diazonium ion

- wherein



Q. 4 Na_2O_2 is pale yellow in colour due to

Option 1:

Presence of traces of superoxides (NaO_2)

Option 2:

O_2^{-2} ion has unpaired electrons.

Option 3:

O_2^{-2} ion is paramagnetic in nature

Option 4:

Its high oxidising power.

Correct Answer:

Presence of traces of superoxides (NaO_2)

Solution:

Properties of Na_2O_2 -

Colourless in pure state, faint yellow is due to presence of small amount of superoxide NaO_2

-

Though O_2^{-2} ion does not have any unpaired electron yet Na_2O_2 is pale yellow in colour due to the presence of traces of NaO_2 .

Correct option is 1.

Q. 5 Which of the following metal cation has least heat of hyd

Option 1:

Li^+

Option 2:

Na^+

Option 3:

K^+

Option 4:

Rb

Correct Answer:

Rb

Solution:

As we learn -

Rb⁺ has minimum charge density .

So its hydration H is minimum.

Q. 6 Which of the following element has the lowest melting po

Option 1:

B

Option 2:

Al

Option 3:

Ga

Option 4:

In

Correct Answer:

Ga

Solution:

As we have learnt,

Melting Point of Boron Family -

Decreases from B to Ga then increases

- wherein

Due to strong crystalline lattice, boron has usually high meltin

Element: B	Al	Ga	In
M.P:	2180	660	30
(OC)			

Melting point of $\approx 30^\circ\text{C}$ is lowest

Q. 7 Which statement is correct for cross Aldol Reaction ?

Option 1:

Reactants must contain

Option 2:

The product of the Reaction is hydroxy Aldehyde or hydroxy Ketone

Option 3:

Condensation carried out between two different Aldehydes or Ketone or one ketone

Option 4:

All of the above

Correct Answer:

All of the above

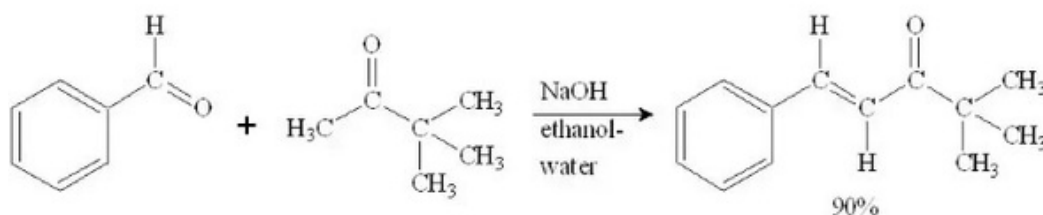
Solution:

As we learned

Cross aldol condensation -

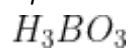
Aldol condensation carried out between two different aldehydes and one ketone.

- wherein

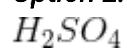


Q. 8 The dilute aqueous solution of which acid is used as a weak antiseptic for eyes and for the treatment of skin diseases.

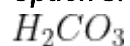
Option 1:



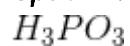
Option 2:



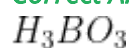
Option 3:



Option 4:



Correct Answer:



Solution:

Boric acid -

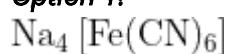
Its dilute solution is used as weak antiseptic for eyes and for the treatment of skin diseases.

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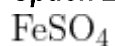
Boric acid in dilute aqueous solution is weak antiseptic for eyes and for the treatment of skin diseases.

Q. 9 In Lassaigne's test of Sulphur containing compound the appearance of a blue color indicates the presence of

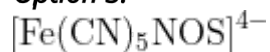
Option 1:



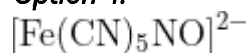
Option 2:



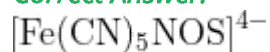
Option 3:



Option 4:



Correct Answer:



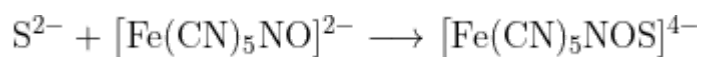
Solution:

As we have learnt,

Test for Sulphur:

In Lassaigne's test of Sulphur containing compound, the violet $[\text{Fe}(\text{CN})_5\text{NOS}]^{4-}$ upon reaction of sodium fusion extract with Nitroprusside ion is formed.

The reaction is given below:



Hence, the correct answer is Option (3)

Q. 10 The primary valency of the central metal in the complex $[\text{Co}(\text{NH}_3)_4\text{Cl}_2]\text{Cl}_2$ is the complex

Option 1:

1

Option 2:

2

Option 3:

3

Option 4:

6

Correct Answer:

2

Solution:

As we have learned

Primary valency -

These are normally ionisable and satisfied by negative ions.

- wherein

eg:

$\text{COCl}_2 \rightarrow$ Primary Valency is 2

$\text{CrCl}_3 \rightarrow$ Primary Valency is 3

Postulates of Werner's theory

Q. 11 Solve the following equation with ~~correct~~ significant figures

Correct Answer:

9.6

Solution:

The number of significant figures in the result would not exceed least number of significant figures.

So, solution is 9.6 as 1.5 has just 2 significant figures

Therefore, Option (1) is correct

Q. 12 At 518°C, the rate of decomposition of a sample of gaseous pressure of 363 Torr, was 1.00 Torr s^{-1} when 5% had reacted. The order of the reaction is :

Correct Answer:

2

Solution:

nth-order reaction -

The rate of the reaction is proportional to the nth power of the

Differential rate law (r)

$$= \frac{dx}{dt} = k(a - x)^n$$

$a - x$ = left amount.

5% reacted means $100 - 5 = 95\%$ left amount

33% reacted means $100 - 33 = 67\%$ left amount

Then

At 363 torr 95% of Total = $a - x = 0.95 P_o$

And after 33% reacted then 67% of Total = $a - x = 0.67 P_o$

Let rate law be:

$$r = K [\text{Acetaldehyde}]^n$$

after 5% reaction

$$\therefore 1 = K (0.95 P_o)^n$$

After 33% reaction

$$0.5 = K (0.67 P_o)^n$$

$$\text{So } 2 = \left(\frac{0.95}{0.67} \right)^n \Rightarrow 2 = (1.41)^n$$

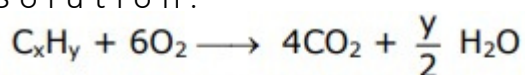
$$\therefore n = 2$$

Q. 13 The formula of a gaseous hydrocarbon which requires 6 times of O_2 for complete oxidation and produces 4 times CO_2 . The value of y is -----.

Correct Answer:

8

Solution:



Applying POAC on 'O' atoms

$$6 \times 2 = 4 \times 2 + \frac{y}{2} \times 1$$

$$\frac{y}{2} = 4 \Rightarrow y = 8$$

Answer : 8

Q. 14 What is the total number of moles if we have a mixture of _____ and 10g Hydrogen?

Correct Answer:

8

Solution:

$$\text{Number of moles of ammonia} = \frac{\text{mass of ammonia}}{\text{molar mass of ammonia}} = \frac{34}{17} = 2$$

$$\text{Number of moles of benzene} = \frac{78}{78} = 1$$

$$\text{Number of moles of hydrogen} = \frac{10}{2} = 5$$

$$\text{Total number of moles} = 2 + 1 + 5 = 8$$

Therefore, Option(1) is correct

Q. 15 Calculate the number of atoms of oxygen present in 88 g of CO₂. What would be the mass (in gm) of CO having the same number of oxygen atoms?

Correct Answer: 112

Solution:

LAWS OF CHEMICAL COMBINATIONS -

Law of Multiple Proportions :

This law was proposed by Dalton in 1803. According to this law, more than one compound, the masses of one element that combine with a fixed mass of another element, are in the ratio of small whole numbers.

-

$$\text{No. of moles of CO}_2 = 88 / (44 \text{ g/mol}) = 2 \text{ moles}$$

As one mole of CO₂ contains two moles of oxygen atoms, so two moles of CO₂ contain 4 moles of oxygen atoms.

$$\text{Number of oxygen atoms} = 4 \times 6.023 \times 10^{23} = 2.5092 \times 10^{24}$$

As 1 mole oxygen atoms present in 1 mole of CO so, 4 moles oxygen atoms are present in 4 moles of CO.

$$\text{It's mass is } 4 \times 28 = 112 \text{ g.}$$

(correct option is a.)

M a t h s

Q. 1 Which of the following is a paradox :

Option 1:

That yellow car is running at 60 Km /h

Option 2:

My car is chauffeur driven

Option 3:

The black car over there is running fast

Option 4:

None

Correct Answer:

The black car over there is running fast

Solution:

As we have learned

Statement -

A sentence which is both true or false is not a statement rather

- wherein

Example: "I must be cruel to be kind."

Q. 2
$$I = \int \frac{x^2}{(x^3 + 1)^4} dx$$

Option 1:

$$\frac{1}{9(x^3 + 1)^3} + C$$

Option 2:

$$\frac{1}{3(x^3 + 1)^3} + C$$

Option 3:

$$-\frac{1}{3(x^3 + 1)^3} + C$$

Option 4:

$$-\frac{1}{9(x^3 + 1)^3} + C$$

Correct Answer:

$$-\frac{1}{9(x^3 + 1)^3} + C$$

Solution:

As we have learned

Type of integration by substitution -

$$\int (f(x))^n \cdot f'(x) dx$$

$$\therefore \frac{[f(x)]^{n+1}}{n+1} + c$$

- wherein

$$\text{Let } f(x) = t$$

$$f'(x) dx = dt$$

$$\text{put : } x^3 + 1 = u \Rightarrow dx = \frac{1}{3x^2}$$

$$I = \frac{1}{3} \int 1/u^4 du$$

$$\int u^n du = \frac{u^{n+1}}{n+1} \text{ heren} = -4$$

$$I = \frac{1}{3} \left[\frac{4^{-4+1}}{-4+1} \right] = -\frac{1}{9u^3}$$

$$\frac{-1}{9(x^3 + 1)^3} + C$$

Q. 3 The value of $\lim_{x \rightarrow 0} (\sin x + \cos(3x))^{2/x}$ is

Option 1:

$$e$$

Option 2:

$$e^{-2}$$

Option 3:

$$e^2$$

Option 4:

$$1/e$$

Correct Answer:

$$e^2$$

Solution:

$$\lim_{x \rightarrow 0} (1 + \sin x + \cos(3x) - 1)^{2/x}$$

$$\Rightarrow e^{\lim_{x \rightarrow 0} \frac{2(\sin x + \cos(3x) - 1)}{1}}$$

Apply L' hospital rule

$$\Rightarrow e \lim_{x \rightarrow 0} \frac{2(\cos x) - 3 \sin(3x)}{1}$$

$$= e^2$$

Q. 4 $\frac{d}{dx}(2x^2 - 3x) = ?$

Option 1:

$$4x - 3$$

Option 2:

$$4x$$

Option 3:

$$4x + 3$$

Option 4:

$$-4x + 3$$

Correct Answer:

$$4x - 3$$

Solution:
As we have learnt,

Rule for differentiation -

The derivative of constant times a function is constant times the

- wherein

$$\frac{d}{dx}(c \cdot f(x)) = c \cdot \frac{d}{dx}f(x)$$

$$\begin{aligned}\frac{d}{dx}(2x^2 - 3x) &= \frac{d}{dx}(2x^2) - \frac{d}{dx}(3x) \\ &= 2\frac{d}{dx}(x^2) - 3\frac{d}{dx}(x) \\ &= 4x - 3\end{aligned}$$

Q. 5 Find the geometric mean of the new observations obtained by 7 whole geometric mean was 14.

Option 1:

9 8

Option 2:

2

Option 3:

2 8

Option 4:

None of these

Correct Answer:

9 8

Solution:
As we learned

Properties of Geometric Mean -

Multiplying each observation by a non-zero constant multiplies constant.

$$G' = (x_1 x_2 x_3 \cdots x_n)^{\frac{1}{n}} \cdot (k^n)^{\frac{1}{n}}$$

$$= (x_1 x_2 x_3 \cdots x_n)^{\frac{1}{n}} k = kG$$

-

$$G' = 7 \times 14$$

$$= 98$$

Q. 6 How many squares are present in a chessboard?

Option 1:

204

Option 2:

$$\sum_{r=1}^8 r^3$$

Option 3:

64

Option 4:

144

Correct Answer:

204

Solution:

Number of squares -

Number of squares of various size from

$$\sum_{r=1}^n r^2$$

- wherein

$$\sum_{r=1}^n r^2 = 1^2 + 2^2 + \dots + n^2$$

Here $n = 8$

$$Sum = 1^2 + 2^2 + \dots + 8^2$$

$$= (8 * 9 * 17) / 6$$

$$= 204$$

Q. 7 Differential equation $y^3 \frac{d^2y}{dx^2} + 2 \left(\frac{dy}{dx} \right)^2 = 0$, where a, b are constant.

Option 1:

$$y^2 \frac{d^2y}{dx^2} + 2 \left(\frac{dy}{dx} \right)^2 = 0$$

Option 2:

$$y^2 \frac{dy}{dx} = 3x$$

Option 3:

$$2 \frac{d^2y}{dx^2} + y \left(\frac{dy}{dx} \right)^2 = 0$$

Option 4:

$$y \frac{d^2y}{dx^2} + 2 \left(\frac{dy}{dx} \right)^2 = 0$$

Correct Answer:

$$y \frac{d^2y}{dx^2} + 2 \left(\frac{dy}{dx} \right)^2 = 0$$

Solution:

As we learnt

Differential Equations -

An equation involving independent variable (x), dependent variable y and its derivatives with respect to independent variable

$$\left(\frac{dy}{dx} \right)$$

- wherein

e.g:

$$\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + 5x = 0$$

Di erentiating $y^3 = 9a(x + b)$ wrt x

$$3y^2 \frac{dy}{dx} = 9a \text{ i.e. } y^2 \frac{dy}{dx} = 3a$$

Again di erentiating wrt x

$$y^2 \frac{d^2y}{dx^2} + 2y \left(\frac{dy}{dx} \right)^2 = 0$$

OR

$$y \frac{d^2y}{dx^2} + 2 \left(\frac{dy}{dx} \right)^2 = 0$$

The elimination of arbitrary constant leads to formation of di e

Q. 8 $f(x) = \sin^{-1} x + \cos^{-1} x$ is di erentiable in:

Option 1:

$$x \in \left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$$

Option 2:

$$x \in [0, \pi]$$

Option 3:

$$x \in \left[0, \frac{\pi}{2} \right]$$

Option 4:

$$x \in [-1, 1]$$

Correct Answer:

$$x \in [-1, 1]$$

Solution:

As we have learnt in

Properties of di erentiable functions -

Trigonometric and inverse trigonometric functions are di erenti

$f(x) = \sin^{-1} x + \cos^{-1} \frac{x}{2}$
 has $[-1, 1]$ common domain

-

Q. 9 The product $4^{1/16} \cdot 8^{1/48} \cdot 16^{1/128} \dots$ is equal to :

Option 1:

$$2^{1/4}$$

Option 2:

$$2$$

Option 3:

$$2^{1/2}$$

Option 4:

$$1$$

Correct Answer:

$$2^{1/2}$$

Solution:

Sum of an infinite GP

If a is the first term and r is the common ratio of a G.P. Then,

$$S_{\infty} = \frac{a}{1-r}$$

S_{∞} is the sum to infinite terms of the G.P.

Now,

$$2^{1/4} \cdot 4^{1/16} \cdot 8^{1/48} \dots = 2^{\frac{1}{4} + \frac{1}{8} + \frac{1}{16} \dots}$$

$$\Rightarrow 2^{\frac{1}{1-1/2}} = \sqrt{2}$$